

Supporting Information

Size-Dependent H and H₂ Formation by Infrared Multiple Photon Dissociation Spectroscopy of Hydrated Vanadium Cations, V⁺(H₂O)_n, n = 3–51

Jakob Heller, Ethan M. Cunningham, Jessica C. Hartmann, Christian van der Linde, Milan

Ončák,* and Martin K. Beyer*

Institut für Ionenphysik und Angewandte Physik, Universität Innsbruck, Technikerstraße 25,
6020 Innsbruck, Austria

Corresponding authors: milan.oncak@uibk.ac.at, martin.beyer@uibk.ac.at

Contents

IRMPD Spectra of Small Clusters.....	2
Ligand Fragmentation.....	3
References.....	4
Cartesian structures of optimized ions (Å) along with ZPE-corrected energies (Hartree)	4
IR frequencies (in cm ⁻¹ , without shift) and intensities (KM/mole) for optimized structures	12

IRMPD Spectra of Small Clusters

The measured IRMPD spectra below, along with the simulated structures and spectra, are consistent with findings from Ohashi and Duncan.^{1,2} A direct comparison between IRMPD spectra of the present study with those measured by Duncan can be found in Figure 1 of the main article.

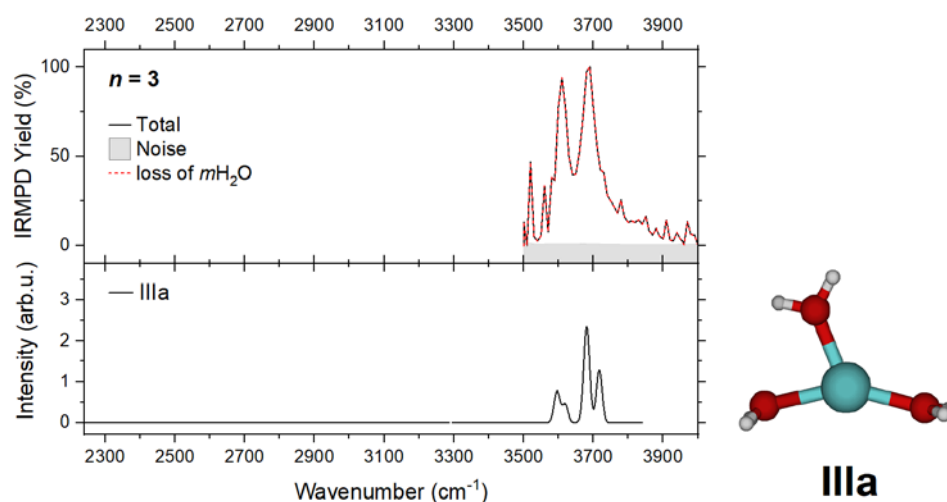


Figure S1. Infrared multiple photon dissociation spectrum of the $V^+(H_2O)_3$ complex along with the simulated spectra of the low-lying intact (IIIa) isomer calculated at the B3LYP/aug-cc-pVDZ level of theory.

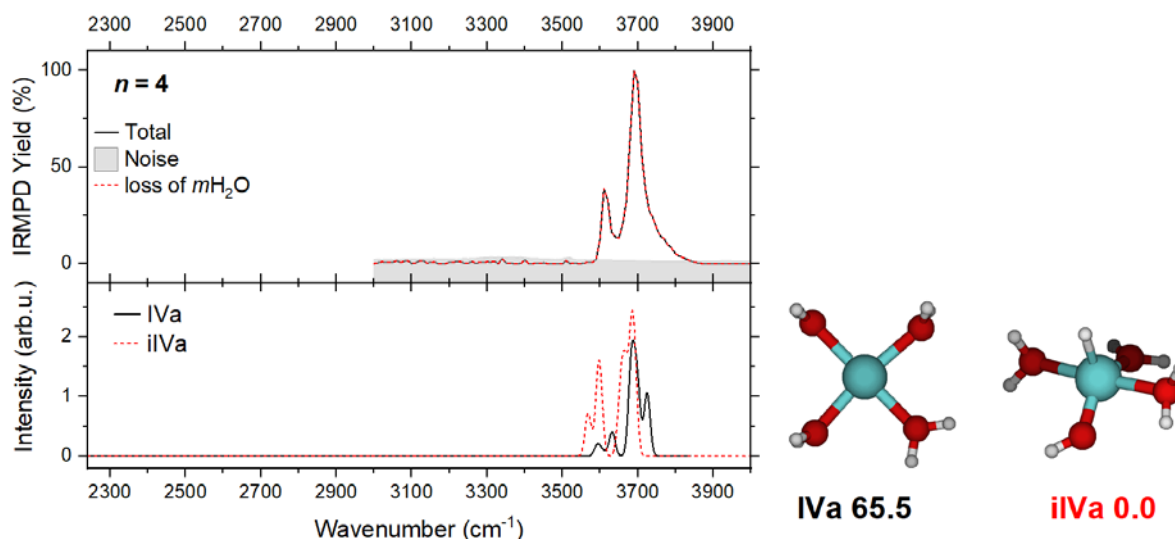


Figure S2. Infrared multiple photon dissociation spectrum of the $V^+(H_2O)_4$ complex along with the simulated spectra of the low-lying intact (IVa) and inserted (iiVa) isomers calculated at the B3LYP/aug-cc-pVDZ level of theory. Structural isomers also show relative energies given in kJ mol⁻¹ inclusive of zero-point energy.

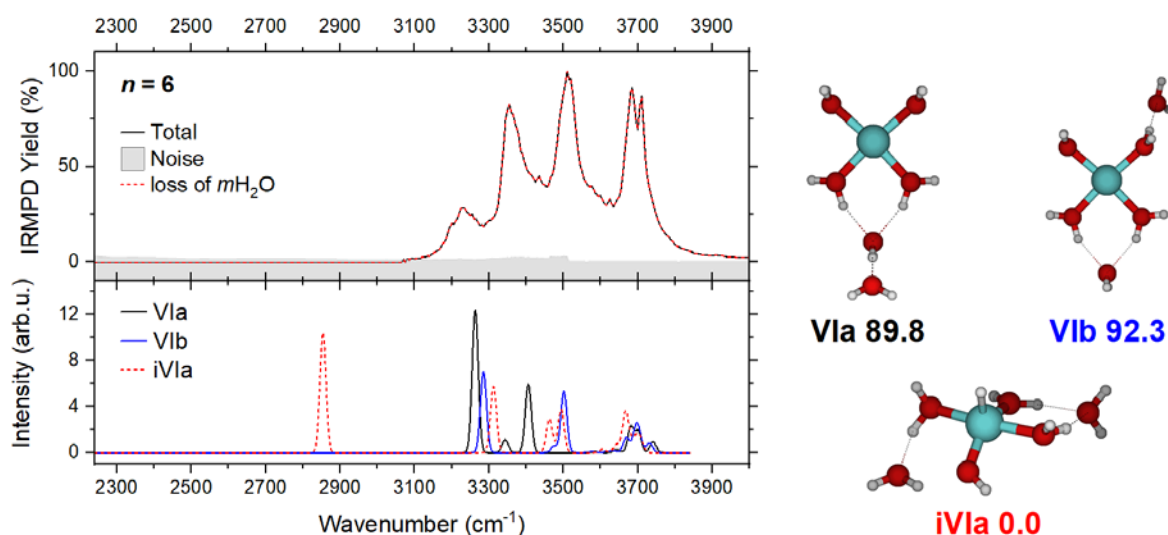


Figure S3. Infrared multiple photon dissociation spectrum of the $V^+(H_2O)_6$ complex along with the simulated spectra of the low-lying intact (**VIa**, **VIb**) and inserted (**iVIa**) isomers calculated at the B3LYP/aug-cc-pVDZ level of theory. Structural isomers also show relative energies given in kJ mol^{-1} inclusive of zero-point energy.

Ligand Fragmentation

Table S1 – Number of ligands lost during the IRMPD process for each cluster size, $V^+(H_2O)_n$ ($n = 3\text{--}12$, 14, 15, 20, 25, 30, 42 and 51), consistent with measured black body infrared dissociation (BIRD) values.³

$V^+(H_2O)_n$	$m(H_2O)$	$H + x(H_2O)$	$H_2 + y(H_2O)$
3	1	–	–
4	1	–	–
5	1	–	–
6	1,2	–	–
7	1,2	–	–
8	1,2	–	1
9	1,2	0,1	1,2
10	1,2	0,1	2
11	1,2	0,1	1,2
12	1	–	2,3
14	1	–	2,3,4
15	1,2,3	–	3
20	1,2,3,4	–	–
25	1,2,3,4	–	–
30	1,2,3,4,5	–	–
42	1,2,3	–	–
51	1,2,3	–	–

References

- 1 J. Sasaki, K. Ohashi, K. Inoue, T. Imamura, K. Judai, N. Nishi and H. Sekiya, *Chem. Phys. Lett.*, 2009, **474**, 36.
- 2 P. D. Carnegie, J. H. Marks, A. D. Brathwaite, T. B. Ward and M. A. Duncan, *J. Phys. Chem. A*, 2020, **124**, 1093.
- 3 B. S. Fox, I. Balteanu, O. P. Balaj, H. C. Liu, M. K. Beyer and V. E. Bondybey, *Phys. Chem. Chem. Phys.*, 2002, **4**, 2224.

Cartesian structures of optimized ions (Å) along with ZPE-corrected energies (Hartree)

IIIa

E = -1173.103678
O 2.330794 -0.132725 -0.000142
V 0.213123 -0.142249 0.000179
O -1.058361 1.591990 -0.000542
O -1.739995 -1.130670 0.000002
H -2.062824 -1.611282 -0.775974
H -2.061265 -1.615427 0.774030
H 2.903368 -0.096855 -0.780030
H 2.903689 -0.096167 0.779475
H -2.023711 1.535106 0.002890
H -0.820593 2.527587 0.000955

IVa

E = -1249.557986
O -0.521866 -2.071034 0.000138
V 0.004612 0.029990 -0.000030
O -2.159259 0.417555 -0.000289
O 0.569618 2.148692 0.000194
O 2.091808 -0.657801 0.000130
H 0.098495 -2.810769 0.002927
H -1.414797 -2.437914 -0.001204
H 2.662546 -0.544535 0.773527
H -2.625454 0.759361 0.775737
H 2.659965 -0.551879 -0.776211
H -2.624621 0.762328 -0.775499
H 0.645717 2.717683 0.777783
H 0.649667 2.716649 -0.777759

iIVa

E = -1249.582933
O -2.114704 -0.203523 0.193675
V -0.012727 0.103277 0.211674
O 0.246513 -1.841736 -0.462338
O -0.356143 1.637637 -0.658842
O 2.131221 0.199309 0.196030
H -2.586129 -0.315844 1.032578
H -2.519960 0.561016 -0.249296
H 0.257915 2.338005 -0.917522
H -0.462381 -2.439138 -0.742144
H 2.511194 0.401631 1.064365
H 2.654864 0.685668 -0.457349
H 0.086844 0.347917 1.848531
H 1.095281 -2.288119 -0.595873

Va

E = -1326.000340
O 2.041927 -1.655097 0.014051
V 0.597029 0.000103 0.000988
O -0.986991 -1.473599 -0.049081

O 2.042016 1.655169 0.013784
O -0.987281 1.473579 -0.047125
H 2.547058 -1.917840 -0.768255
H 2.578689 -1.883183 0.785862
H -1.928787 -1.230014 0.007023
H 2.554802 1.911434 -0.765685
H -0.904265 -2.427076 0.066670
H 2.572904 1.886046 0.788860
H -1.929803 1.232008 0.004805
H -0.904174 2.428879 0.051789
O -3.402052 -0.000225 0.035025
H -3.991535 -0.001638 -0.732394
H -3.987505 0.000406 0.805363

Vb

E = -1325.997426
O 3.679063 -0.141104 -0.608385
V -0.602970 0.027119 0.137021
O 1.426203 0.511915 0.715977
O -0.891302 2.181174 -0.122546
O -0.269479 -2.134473 0.227668
O -2.631020 -0.471648 -0.567220
H 4.341544 0.490471 -0.915156
H 3.944892 -1.000684 -0.957409
H -0.090278 2.724024 -0.116070
H 0.093274 -2.575612 1.007813
H -1.567806 2.689253 0.345861
H -0.937443 -2.730489 -0.138327
H -2.951829 -0.170668 -1.429393
H -3.393903 -0.469867 0.028664
H 2.236982 0.248782 0.216892
H 1.685165 0.604141 1.641692

Vc

E = -1325.988819
O 1.903491 -0.021790 -0.266750
H 2.602523 0.590917 -0.525972
H 2.298538 -0.921798 -0.179162
V -0.051691 0.662188 0.202049
O 0.902576 2.570157 -0.362874
H 0.629493 3.025146 -1.172329
H 1.029008 3.257453 0.306776
O -1.815029 -0.232689 0.844801
H -2.550135 -0.612185 0.296120
H -2.047778 -0.359470 1.773698
O 2.929349 -2.488822 -0.018927
H 3.456766 -2.797823 0.728331
H 3.138644 -3.075273 -0.756692
O -3.779523 -1.247184 -0.621195
H -3.893773 -2.175299 -0.860498

H -4.601304 -0.799358 -0.857824

iVa

E = -1326.030297
O 0.495591 -1.884174 0.384740
V -0.670272 -0.115809 0.231817
O -1.765206 1.733748 0.074854
O 0.975251 1.044336 -0.032199
O -1.665100 -1.088987 -0.921599
O 3.476941 0.348447 -0.265727
H 0.667418 -2.273675 1.253937
H 0.023312 -2.556215 -0.134890
H 1.934231 0.768371 -0.128639
H 0.917138 2.004262 -0.128176
H -2.490577 -0.845600 -1.360088
H -2.291558 1.914016 0.868037
H 3.911121 0.087698 -1.088053
H 4.178048 0.559045 0.364239
H -1.257398 -0.194418 1.785997
H -2.315294 1.973173 -0.684717

iVb

E = -1326.028389
O 1.189867 1.603017 -0.763277
V 0.443702 -0.006115 0.307703
O -0.487166 -1.493618 -0.178824
O -1.248969 1.150815 0.632433
O 2.388194 -0.867001 -0.097285
O -3.004182 -0.308127 -0.527930
H 2.079577 1.712736 -1.127097
H 0.667656 2.394560 -0.959606
H -2.077196 0.696613 0.268856
H 2.889112 -1.071783 0.706144
H -1.437299 1.427347 1.539800
H 2.571792 -1.574655 -0.731575
H -2.469459 -1.121950 -0.513840
H -0.110442 -2.375930 -0.296053
H -3.926540 -0.550295 -0.381165
H 0.905685 -0.076679 1.896433

iVc

E = -1326.022934
O 1.876631 -1.303453 -0.595273
V 0.386890 -0.071533 0.248903
O -1.010334 1.414799 0.157512
O -0.774039 -1.456155 0.461519
O 1.880314 1.439375 -0.260981
O -2.983137 -0.006926 -0.623936
H 1.711810 -2.252090 -0.690784
H 2.831670 -1.162536 -0.539247
H -2.698193 -0.872696 -0.286471
H 1.831504 2.092652 -0.973271
H -0.796741 -1.972544 1.279553
H 2.335907 1.855805 0.484219
H -1.912100 1.037415 -0.099422
H -1.124537 2.044254 0.882046
H -3.946979 0.004830 -0.661367
H 0.953696 0.169055 1.769253

VIa

E = -1402.439937
O 2.664644 -1.651958 -0.258946
V 1.235792 0.000150 -0.002736
O -0.339140 1.458748 0.223022
O -0.339372 -1.458199 0.223124
O 2.665848 1.651059 -0.259498
O -2.588223 0.000488 0.854852
H 3.001374 -1.922740 -1.124699
H 3.351458 -1.860521 0.389448
H -1.236606 -1.169584 0.493389
H 3.002816 1.920943 -1.125439
H -0.238916 -2.396321 0.419086
H 3.353125 1.858752 0.388684
H -1.236481 1.170466 0.493291
H -0.238385 2.396859 0.418905

H -3.370192 0.000445 0.252607
H -2.950341 0.000542 1.750209
O -4.742317 -0.000295 -0.788532
H -5.216485 0.771013 -1.122606
H -5.216105 -0.772039 -1.122135

VIb

E = -1402.438963
O 1.804480 -0.724175 0.796868
V -0.000826 0.321270 0.199891
O -1.880556 1.188439 -0.463432
O -1.042011 -1.581518 0.182914
O 0.865104 2.340090 0.074250
O -3.766093 -0.932472 -0.275448
H 2.618916 -0.814780 0.249593
H 2.072083 -0.777553 1.722821
H -2.011268 -1.641636 0.109322
H 1.480678 2.561099 -0.639677
H -0.703777 -2.413927 0.532717
H 1.194120 2.780631 0.870804
H -2.710763 0.680430 -0.422650
H -2.095171 2.128285 -0.431427
H -4.193759 -1.240542 -1.086882
H -4.449678 -0.982713 0.407222
O 4.002839 -0.948596 -0.796457
H 4.023252 -1.591884 -1.516507
H 4.924263 -0.810760 -0.542390

iVIa

E = -1402.474132
O 1.150201 -1.347323 0.488387
V 0.129463 -0.204151 -0.500786
O -1.042682 1.366279 0.113934
O -1.638537 -1.411632 -0.255729
O 1.684835 1.175433 -0.707961
O 3.347536 0.223112 1.006091
O -3.549164 0.506645 0.720614
H 0.128985 -0.643856 -2.102375
H 0.784333 -2.181201 0.814872
H 2.021064 1.323629 -1.602001
H 2.471794 0.931750 -0.122941
H -0.692187 2.251857 0.280104
H -1.981220 1.300467 0.401056
H -2.482014 -1.010708 0.023052
H -1.826880 -2.012109 -0.989968
H -3.859118 0.432145 1.635110
H -4.321182 0.797328 0.213396
H 2.867887 -0.627547 1.039823
H 4.293376 0.033609 1.005253

VIIIa

E = -1555.316971
O 1.508037 1.533991 -0.062419
V -0.044503 -0.002970 -0.214097
O -1.596065 1.521618 -0.405458
O 1.499213 -1.546646 -0.046243
O -1.600953 -1.524083 -0.386914
O -3.908361 0.000365 -0.630597
O -5.696331 0.013338 1.409869
O 3.784584 -0.016500 -0.494393
H 1.512925 2.113755 0.711044
H 2.418747 1.184327 -0.165198
H -2.507374 1.184120 -0.538464
H 1.501076 -2.112473 0.737547
H -1.469719 2.259854 -1.015156
H 2.411437 -1.203022 -0.154393
H -2.511012 -1.185324 -0.524808
H -1.476462 -2.271027 -0.986291
H -4.546132 0.006419 0.122093
H -4.452068 -0.001658 -1.428664
H -6.016711 -0.755231 1.897639
H -6.019860 0.787947 1.885859
H 4.605072 -0.003152 0.051588
H 4.086267 -0.008393 -1.412466
O 6.053250 0.020321 1.014646

H 6.555073 0.797351 1.289621
H 6.585321 -0.744421 1.266344

VIIIb

E = -1555.316095
O -1.110662 -1.810721 -0.511910
V 0.535772 -0.439403 -0.077980
O 1.936772 -2.079527 0.317692
O -0.802394 1.195185 -0.544840
O 2.090560 0.989704 0.449744
O -3.270618 -0.069803 -0.812652
O 4.430331 -0.680286 0.133269
O 0.807824 3.525193 0.054661
H -1.964133 -1.361347 -0.692225
H -0.990466 -2.480180 -1.198082
H 2.872145 -1.801689 0.348776
H -1.766524 1.048693 -0.577676
H 1.778780 -2.622877 1.102255
H -0.602420 2.112374 -0.302277
H 3.020204 0.762939 0.284572
H 1.945634 1.932693 0.261107
H 5.139987 -0.707149 0.790064
H 4.870207 -0.799782 -0.720130
H -3.979041 -0.121268 -0.130952
H -3.731433 0.016092 -1.656876
H 0.739229 4.082603 0.841888
H 0.971762 4.137815 -0.675349
O -5.243834 -0.253645 1.064214
H -5.565024 -1.075388 1.455134
H -5.765496 0.453959 1.461890

VIIIc

E = -1555.315237
O 0.686858 -2.062732 -0.285193
V 0.000002 -0.000154 -0.200514
O 2.062764 0.686432 -0.284834
O -2.062674 -0.686645 -0.285331
O -0.686671 2.062523 -0.286079
O -1.745661 -3.487771 0.322506
O 1.745246 3.487971 0.322504
O -3.488128 1.745375 0.322002
H 0.081266 -2.754785 0.029918
H 1.585649 -2.253926 0.031987
H 2.253771 1.585267 0.032395
H -2.253835 -1.585399 0.032043
H 2.754025 0.080534 0.031600
H -2.754401 -0.080860 0.030235
H -0.080872 2.754561 0.028784
H -1.585359 2.253850 0.031387
H 1.959281 3.919638 1.160797
H 2.052001 4.098064 -0.362777
H -1.961007 -3.919094 1.160642
H -2.051629 -4.098019 -0.362994
H -3.919913 1.960805 1.159874
H -4.097936 2.051402 -0.363857
O 3.488314 -1.744861 0.321627
H 4.097264 -2.051159 -0.364881
H 3.921271 -1.959669 1.159059

VIIIId

E = -1555.314445
O -2.967198 1.265891 -0.727024
V -1.306495 0.042537 0.024518
O -0.019650 1.792819 0.115931
O -2.565881 -1.754170 -0.052397
O 0.372006 -1.123098 0.767067
O 2.327359 0.770911 1.095911
O 4.451761 0.726594 -0.467366
O -5.149854 -0.507767 -0.156067
H -2.897674 1.643337 -1.615015
H -3.847947 0.851505 -0.661875
H 0.879364 1.638296 0.484686
H -2.357358 -2.434913 -0.707356
H -0.339028 2.633784 0.465594
H -3.524148 -1.582530 -0.115841

H 1.184068 -0.612028 0.984180
H 0.258442 -1.796128 1.449307
H 3.126781 0.747100 0.500624
H 2.661614 1.019023 1.966782
H 5.139020 0.030534 -0.528233
H 4.710928 1.430203 -1.071811
H -5.889721 -0.735917 -0.736305
H -5.546540 -0.364238 0.715145
O 6.395140 -1.220020 -0.604683
H 7.253417 -1.171729 -0.166177
H 6.488711 -1.883947 -1.298597

iVIIIa

E = -1555.359085
V 0.173830 -0.584076 0.273901
H 1.062098 -1.644020 1.222947
O -0.506090 -1.294835 -1.283632
H 0.039110 -1.261685 -2.081847
O -1.574331 -1.191907 1.315806
H -1.482141 -1.978341 1.868701
H -2.354712 -1.313751 0.727245
O -0.304412 1.328959 0.707370
H -1.277860 1.567428 0.615981
H 0.249258 2.065796 0.378251
O 1.950050 0.107469 -0.602102
H 2.148761 1.059419 -0.612714
H 2.777167 -0.388051 -0.363245
O 4.068179 -1.272350 0.206029
H 3.826533 -1.940147 0.861612
H 4.786629 -1.651582 -0.315766
O 1.707000 2.966714 -0.325958
H 1.592466 3.534492 -1.100839
H 2.247805 3.481827 0.289150
O -3.131296 -0.929230 -0.846899
H -2.287086 -1.152179 -1.310427
H -3.847190 -1.389183 -1.301635
O -2.809769 1.717376 0.133024
H -3.152718 0.897261 -0.275006
H -3.520854 2.088879 0.668768

iVIIIb

E = -1555.357661
O -1.244175 -0.331732 1.410176
V 0.586194 -0.824439 0.522323
O 2.508694 -1.137688 -0.402562
O 0.989604 1.165394 0.411362
O -0.258860 -1.888732 -0.723541
O -1.314989 2.375316 0.720005
O -2.795790 1.411890 -1.251020
O -2.853735 -1.302094 -0.532571
O 3.477083 1.499627 -0.814328
H -2.014066 -0.738769 0.947787
H -1.446482 0.620040 1.496654
H 1.779092 1.550320 -0.015088
H -2.000577 -1.717810 -0.814552
H 0.241024 1.819361 0.484519
H 0.255603 -2.383152 -1.375503
H 3.070565 -0.364528 -0.602859
H 3.053526 -1.779916 0.072620
H 3.594127 1.821579 -1.719556
H 4.216161 1.874527 -0.314205
H -2.994926 0.459335 -1.146919
H -3.536123 -1.983713 -0.562998
H -3.452408 1.779025 -1.853275
H -1.575809 3.212875 1.121329
H -1.933047 2.190305 -0.037431
H 1.198245 -1.733229 1.765886

iVIIIc

E = -1555.357067
O 0.992103 0.134340 1.456383
V -0.710599 0.057110 0.235251
O -2.365838 -0.317608 -1.040191
O -0.110282 -1.813249 -0.297443
O -0.292881 1.698718 -0.502022

O 2.393380 -2.030880 0.360131
O 3.517724 -0.057322 -0.995227
O -4.642585 0.076107 0.224736
O 2.255173 2.160916 0.198406
H 1.555814 0.924833 1.284184
H 1.587853 -0.638905 1.445911
H -0.576150 -2.403460 -0.902668
H 1.356040 2.271556 -0.197339
H 0.834148 -2.108851 -0.146362
H -0.894128 2.185845 -1.079752
H -2.441178 0.045450 -1.931725
H -3.256908 -0.215493 -0.602222
H 3.261580 0.832341 -0.680535
H 2.565887 3.033830 0.468277
H -5.484849 -0.391470 0.161009
H -4.513810 0.286643 1.159197
H 4.317272 0.042014 -1.523962
H 2.940689 -2.775214 0.638128
H 2.956616 -1.416032 -0.182548
H -1.839452 0.205206 1.441455

iVIIIId

E = -1555.353271
O 1.000912 -1.881451 -0.564151
V -0.674119 -0.703756 0.020327
O -2.200479 0.619445 0.640252
O 0.499803 0.932375 -0.334312
O -0.784227 -1.790373 1.459235
O 2.949525 0.066852 -1.017496
O 5.138373 0.374359 0.532248
O -4.261870 -0.165409 -0.811954
O -0.890277 3.232517 0.268216
H 1.109399 -2.643773 0.022189
H 1.869038 -1.448621 -0.686857
H 0.229044 1.859457 -0.176197
H 1.451789 0.847931 -0.582386
H -1.459530 -1.649162 2.137354
H -2.056047 1.577750 0.587342
H -3.069080 0.412243 0.202099
H -0.715724 3.788335 1.040407
H -1.191372 3.840782 -0.421185
H 5.702229 -0.349687 0.832405
H -5.139078 -0.497508 -0.583183
H -3.806264 -0.881694 -1.281013
H 5.653612 1.181310 0.655528
H 3.240352 0.129639 -1.936750
H 3.762883 0.189301 -0.469122
H -1.690606 -1.276430 -1.184473

IXa

E = -1631.753600
O -1.651980 -1.788061 -0.658039
V -0.045427 -0.343544 -0.299676
O 1.483359 1.127156 0.166035
O 1.506016 -1.887951 -0.227795
O -1.520382 1.231601 -0.480147
O -3.932176 -0.173734 -0.514229
O -5.630762 -0.665728 1.570943
O 3.803468 -0.314434 -0.474304
O 0.017628 3.622818 0.023190
H -2.543603 -1.379974 -0.686186
H -1.578282 -2.362040 -1.432041
H 2.410902 -1.510562 -0.266054
H -2.470436 1.032132 -0.388406
H 1.487520 -2.499457 0.520827
H -1.331385 2.143073 -0.208030
H 2.406443 0.920397 -0.072389
H 1.304062 2.070304 0.024046
H 4.591065 -0.386784 0.110345
H 4.151078 -0.293437 -1.375104
H -4.532694 -0.334248 0.248609
H -4.512457 -0.054124 -1.276709
H 0.016702 4.153234 0.831541
H 0.046090 4.264073 -0.699893
H -5.805237 -1.537687 1.945765

H -6.074755 -0.032735 2.148057
O 5.988555 -0.542422 1.162668
H 6.455911 0.173401 1.610140
H 6.514081 -1.338000 1.311463

IXb

E = -1631.753268
O -1.560878 -2.113574 -0.110562
V 0.318923 -1.001096 -0.001629
O 2.099477 0.234454 0.175623
O 1.450003 -2.738455 0.718882
O -0.727376 0.713658 -0.781237
O -3.396205 -0.149940 -0.855503
O -5.425003 0.344155 0.914595
O 4.086327 -1.904631 -0.006903
O 1.247095 2.706350 -0.830512
H -2.319794 -1.570678 -0.415339
H -1.580842 -2.939128 -0.611861
H 2.414767 -2.629730 0.611711
H -1.698339 0.765711 -0.815559
H 1.298205 -3.010205 1.635022
H -0.318169 1.596836 -0.802684
H 2.960170 -0.163324 -0.028078
H 2.049384 1.128412 -0.217446
H 4.882448 -1.961529 0.539405
H 4.342146 -2.267166 -0.866662
H -4.112255 0.047671 -0.210690
H -3.829342 -0.178972 -1.717964
H 1.327511 3.493537 -0.247388
H 1.499044 3.013682 -1.710403
H -5.839621 -0.322299 1.475992
H -5.798874 1.191460 1.184936
O 1.511263 4.921231 0.769025
H 0.876086 5.635122 0.902269
H 2.234626 5.089813 1.384953

IXc

E = -1631.752627
V -0.707014 0.232951 -0.290494
O 0.974019 -1.033394 -0.883393
O 0.721328 1.832809 0.132003
O -2.388316 1.496262 0.325778
O -2.137720 -1.356239 -0.767339
H -2.017585 -1.835594 -1.597417
H -3.077972 -1.080701 -0.730163
H -3.271174 1.099959 0.163985
H -2.387600 1.807754 1.240860
H 0.518084 2.726253 -0.172971
H 1.640982 1.633932 -0.153337
H 1.837912 -0.562010 -0.895427
H 1.111734 -1.847407 -0.381001
O 3.081823 0.728306 -0.762246
H 3.834905 0.581865 -0.127045
H 3.486020 1.020067 -1.588749
O -4.577951 -0.058291 -0.402376
H -5.237587 -0.404330 0.242753
H -5.090459 0.237877 -1.165502
O 5.036551 0.304980 0.971549
H 5.816814 -0.274577 0.844041
H 5.258837 0.915686 1.682787
O -6.392366 -1.007092 1.391364
H -6.626218 -1.933360 1.528003
H -7.011980 -0.492843 1.923216
O 7.192083 -1.365422 0.572358
H 8.029089 -1.125770 0.156119
H 7.371895 -2.160011 1.089607

IXd

E = -1631.749201
O 0.880178 1.863894 -0.137372
V 2.079762 0.043329 -0.094865
O 3.277371 -1.792734 -0.080481
O 3.912919 1.241259 0.005085
O 0.248530 -1.133279 -0.224819
O -1.572892 0.835078 -0.775665

O -3.638909 1.126521 0.807718
 O -5.597252 -0.707322 0.919434
 O 5.910833 -0.772285 0.385160
 H 4.041601 1.951001 -0.638407
 H 4.756227 0.756829 0.073785
 H 4.243316 -1.690817 0.004097
 H 3.118023 -2.458109 -0.763308
 H 0.012271 -1.720698 0.505029
 H -0.546046 -0.583585 -0.418938
 H -0.067801 1.693700 -0.345677
 H 0.900099 2.458021 0.624277
 H -2.382968 0.960767 -0.200258
 H -1.878043 0.925456 -1.686925
 H 6.224217 -0.863397 1.296240
 H 6.690945 -0.919387 -0.167560
 H -4.007113 1.981603 1.054834
 H -4.381852 0.475308 0.850486
 H -5.823113 -1.152614 1.743537
 H -6.408848 -0.713256 0.372468
 O -7.864074 -0.717905 -0.686064
 H -8.114432 -1.449640 -1.263097
 H -8.664631 -0.193553 -0.562666

IXe

E = -1631.748298
 O 0.295103 -1.531764 0.356907
 V 1.825879 0.000042 0.110904
 O 3.361048 -1.551263 -0.100653
 O 0.295099 1.531861 0.356843
 O 3.361081 1.551300 -0.100806
 O -1.807968 -0.000043 1.167491
 O -4.019711 0.000005 -0.188820
 O -5.528597 -2.348222 -0.485667
 O 5.685906 -0.000087 -0.721258
 H 3.399127 -2.257540 0.558246
 H 4.275610 -1.251371 -0.255977
 H 4.275580 1.251256 -0.256186
 H 3.399297 2.257528 0.558134
 H 0.107046 2.131368 -0.377083
 H -0.569427 1.157907 0.650767
 H -0.569413 -1.157839 0.650918
 H 0.107022 -2.131518 -0.376800
 H -2.683639 -0.000046 0.669764
 H -2.034418 0.000034 2.105552
 H 5.936009 -0.000105 -1.656129
 H 6.521953 -0.000020 -0.234706
 H -4.586746 -0.787703 -0.288418
 H -4.586780 0.787705 -0.288389
 H -6.165245 -2.706539 0.144812
 H -5.780865 -2.710036 -1.343992
 O -5.528643 2.348226 -0.485620
 H -5.781949 2.709394 -1.343916
 H -6.164935 2.706457 0.145274

iIXa

E = -1631.798859
 O -1.315653 -0.741757 1.383095
 V 0.488927 -0.495667 0.321003
 O 0.180037 1.505818 0.438008
 O -0.109116 -1.653178 -0.985315
 O 2.263699 -0.066879 -0.751170
 O -2.714832 -1.986056 -0.583139
 O -3.636588 0.635706 -0.930830
 O 4.254356 -1.296733 0.499982
 O -2.355153 1.835400 1.052824
 O 2.181094 2.859765 -0.889105
 H -1.952992 -1.330317 0.917261
 H -1.807200 0.073564 1.600353
 H 0.749142 2.174716 0.005288
 H -1.799126 -2.052657 -0.956725
 H -0.727695 1.856428 0.645174
 H 0.471226 -1.845147 -1.734269
 H 2.497983 0.858203 -0.932255
 H 3.066403 -0.518330 -0.378291
 H 2.062971 3.318783 -1.732386

H 2.814973 3.396524 -0.392912
 H -3.490091 -0.332324 -0.942022
 H -3.130739 -2.852218 -0.669997
 H 4.958946 -1.872323 0.176938
 H 3.838610 -1.760322 1.240448
 H -4.439619 0.811397 -1.433472
 H -2.833270 2.491015 1.574200
 H -2.953074 1.530278 0.318967
 H 1.445485 -1.283627 1.435846

iIXb

E = -1631.798034
 O 0.337112 -1.299614 0.004795
 V -0.672343 0.423439 -0.155837
 O -2.337211 -0.681729 -0.971787
 O 1.030346 1.372981 0.620877
 O -1.806223 1.237115 1.041472
 O 2.740414 -0.815481 1.103817
 O 5.038087 -1.199662 -0.268396
 O 1.694463 3.416402 -0.964178
 O -1.220009 -3.357827 -0.388542
 O -4.251502 0.296221 0.445964
 H 1.238050 -1.355016 0.402383
 H -0.091480 -2.188621 -0.128531
 H -3.179055 -0.434839 -0.466707
 H 1.805615 0.814084 0.823138
 H -2.492567 -0.408019 -1.886900
 H 1.334113 2.164088 0.107356
 H -3.580578 0.808820 0.948856
 H -1.425021 1.862696 1.672633
 H -4.860443 -0.100518 1.079804
 H 3.583690 -0.966383 0.612496
 H 2.929187 -1.040814 2.023804
 H 1.090442 3.409987 -1.719167
 H 1.835931 4.344785 -0.739772
 H 5.414040 -2.042473 -0.551018
 H 5.732830 -0.541192 -0.392588
 H -1.957912 -2.883009 -0.800125
 H -1.164023 -4.223734 -0.810174
 H -0.552749 1.293805 -1.583405

iIXc

E = -1631.796709
 O -2.071847 -1.545784 -1.153587
 V -0.658715 -0.139079 -0.402969
 O 0.842145 -1.622963 -0.433233
 O -1.994688 1.106034 -0.052878
 O 0.838012 1.101555 0.451464
 O -3.733621 -0.663411 0.776970
 O -1.143984 -1.211688 1.565454
 O 3.104310 -0.176044 -0.627160
 O 5.465079 -0.595900 0.646343
 O -0.153818 3.627089 -0.052975
 H -2.926053 -1.438937 -0.677241
 H -2.248449 -1.460574 -2.099692
 H 1.783442 -1.341897 -0.495960
 H -3.379659 0.233306 0.543550
 H 0.770802 -2.481501 -0.000023
 H -1.789128 2.050179 -0.016018
 H 1.733665 0.900128 0.113465
 H 0.657979 2.053667 0.299518
 H 3.970494 -0.317224 -0.177661
 H 3.312719 0.029955 -1.547738
 H -2.120067 -1.175170 1.647843
 H -4.658079 -0.577978 1.036178
 H -0.135223 4.386560 0.543843
 H -0.099214 3.995416 -0.944879
 H -0.789833 -0.831727 2.379782
 H 5.994704 0.070395 1.101432
 H 6.038055 -1.365549 0.541168
 H -0.178424 0.318678 -1.942466

iIXd

E = -1631.796120
 O -0.475105 1.093354 0.686979

V 0.715860 -0.468968 0.149438
O 2.370253 0.758744 0.524497
O -1.085708 -1.518129 -0.253374
O 1.444709 -1.003195 -1.447991
O -3.044538 0.451504 0.431879
O -4.631641 1.428073 -1.524499
O -0.875341 -3.690637 1.268134
O 1.077516 3.283331 1.311278
O 3.839362 0.292128 -1.564077
H -1.463810 1.058406 0.656657
H -0.134051 1.980064 0.923635
H 3.090959 0.675463 -0.167863
H -1.923912 -1.051801 -0.079652
H 2.266954 1.690868 0.769085
H -1.120180 -2.388662 0.220168
H 3.135503 -0.338940 -1.828313
H 0.942836 -1.613765 -2.004836
H 4.679846 -0.178154 -1.618269
H -3.639594 0.821488 -0.264437
H -3.602110 0.303794 1.206433
H -0.902986 -4.639126 1.090845
H -0.002526 -3.504263 1.645794
H -5.092903 2.275555 -1.549282
H -5.040910 0.881087 -2.206650
H 1.181006 3.589262 2.223085
H 1.148950 4.078104 0.764784
H 1.056084 -1.614499 1.319130

H2O
E = -76.423418
O 0.000000 0.000000 0.117802
H -0.000000 0.764237 -0.471206
H -0.000000 -0.764237 -0.471206

H
E =
H 0.000000 0.000000 0.000000

H2
E = -1.164102
H 0.000000 -0.000000 0.380433
H 0.000000 -0.000000 -0.380433

V+(H2O)7
E = -1478.878329
O -2.123928 -1.556000 0.320856
V -0.620010 -0.000051 -0.034483
O -2.123656 1.556188 0.321324
O 0.901576 1.517798 -0.396507
O 0.901986 -1.517082 -0.396797
O 3.175027 0.000085 -0.859025
O 5.152405 -0.000516 0.994611
H -2.027442 -2.136033 1.088752
H -3.051378 -1.253416 0.306363
H 1.796102 -1.181238 -0.621527
H -2.026309 2.138025 1.087737
H 0.721614 -2.270710 -0.972879
H -3.051199 1.253912 0.308404
H 1.795740 1.181754 -0.620651
H 0.721436 2.270781 -0.973514
H 3.887124 -0.000125 -0.175809
H 3.633825 0.000581 -1.708842
H 5.555550 0.771244 1.410657
H 5.555019 -0.772284 1.411156
O -4.517574 -0.000431 0.066291
H -5.274321 -0.002108 0.669186
H -4.902221 0.000447 -0.821949

HVOH+(H2O)6
E = -1478.917497
V -0.151336 -0.892274 -0.380030
H -0.450864 -2.168297 -1.412129
O 0.706536 -1.329401 1.186140
H 0.202288 -1.647546 1.947614
O 1.690143 -0.527212 -1.337583

H 2.005462 -1.212988 -1.940826
H 2.414912 -0.303624 -0.707363
O 2.860982 0.278958 0.923261
H 3.704943 0.189818 1.382859
H 2.225862 -0.352981 1.337319
O 1.316386 2.522944 0.087335
H 2.008308 1.944615 0.465064
H 1.763424 3.247942 -0.365926
O -0.669756 1.040727 -0.668393
H 0.063657 1.710637 -0.493784
H -1.521426 1.391854 -0.344594
O -3.307929 1.321854 0.315701
H -4.008282 1.559615 -0.308775
H -3.530571 1.785834 1.135484
O -2.106491 -1.202707 0.427430
H -2.565975 -1.997522 0.125557
H -2.749987 -0.466348 0.449051

VOH+(H2O)4
E = -1325.454518
O 1.996174 0.884367 -0.050629
V 0.099944 -0.180795 -0.065913
O -0.633408 1.233297 1.457863
O -1.123811 1.181730 -1.318768
O 1.366308 -1.571134 -0.077907
O -1.697660 -1.379443 0.177755
H 2.394525 1.475141 -0.702235
H 2.498868 0.041644 -0.066126
H -1.448632 2.022260 -0.966108
H -1.072533 1.278352 -2.278540
H 1.375266 -2.529400 0.000301
H -1.598119 -2.322235 0.369384
H -2.468377 -1.295673 -0.400160
H 0.045605 1.733201 1.933578
H -1.286141 0.964447 2.119406

VOH+(H2O)5
E = -1401.904594
O 1.359888 1.417852 -0.935355
V 0.020338 -0.019943 0.027738
O 1.708073 -0.227950 1.453787
O -1.688039 0.130658 -1.043249
O 0.933698 -1.634251 -1.124540
O -0.975961 1.818499 0.681867
O -1.388483 -1.464655 0.875944
H 1.734170 1.265550 -1.813668
H 1.011335 2.321344 -0.933511
H 0.323709 -2.167742 -1.653082
H -1.679159 1.553029 0.028421
H 1.566200 -2.251841 -0.733040
H -1.395678 2.097168 1.504693
H -1.854695 -1.517740 1.718834
H -2.023886 -1.148621 0.182515
H -1.859014 0.170516 -1.988273
H 1.685753 -0.599047 2.344856
H 2.430082 0.414849 1.436638

VOH+(H2O)6
E = -1478.352832
O 1.872588 -0.208401 -1.536841
V 0.364853 0.015859 0.035080
O -1.052480 0.492730 1.634484
O -0.838769 -1.558134 -0.494943
O 1.610212 1.675158 0.800369
O -0.778685 1.382227 -1.207542
O 1.290536 -1.743798 0.948918
O -2.867738 -0.023751 -0.237475
H 1.663005 0.009634 -2.455152
H 2.391440 -1.024547 -1.554855
H -0.745626 2.344791 -1.143977
H 1.533770 -2.020590 1.840417
H -1.721821 1.112395 -1.113156
H 0.503848 -2.258619 0.647453
H -1.083444 0.019053 2.474743
H -1.942600 0.377786 1.216944

H 2.526610 1.856883 0.557038
H 1.415002 2.189222 1.593931
H -0.774395 -1.994301 -1.352009
H -3.786306 -0.284729 -0.368485
H -2.256417 -0.819979 -0.405486

VOH+(H2O)7

E = -1554.797986
O 0.528149 -2.176145 -0.124675
V 0.499913 0.000749 0.043714
O 2.115308 0.002242 1.539103
O 0.521171 2.177312 -0.127388
O -1.142652 -0.001318 1.318334
O 2.138808 0.002539 -1.440445
O -0.994983 -0.003493 -1.543836
O -2.101010 2.045935 0.011867
O -2.095655 -2.049639 0.011090
H -0.415582 -2.472242 -0.066286
H 1.042105 -2.748432 0.457449
H -1.580492 -0.774635 -1.411107
H 3.053875 0.005882 1.311638
H -1.581801 0.767488 -1.418533
H 2.050585 0.005782 2.501823
H 1.033306 2.753273 0.452668
H -0.424065 2.469280 -0.068482
H 2.174812 -0.770306 -2.021670
H 2.173653 0.774649 -2.022695
H -1.078396 -0.001432 2.278880
H -2.891091 2.550456 0.235247
H -1.961812 1.319410 0.691628
H -2.887994 -2.552543 0.230062
H -1.958199 -1.323317 0.691566

VOH+(H2O)8

E = -1631.238884
O -0.280123 -2.092908 0.316808
V 0.726333 -0.168140 0.098232
O -0.578289 0.248111 -1.574035
O 2.192257 -0.675949 1.663859
O 1.834589 1.615985 -0.525166
O -0.542054 0.948824 1.301504
O 2.104089 -1.299421 -1.217651
O -2.598838 -1.499971 -0.848064
O -0.532334 2.808517 -0.537855
O -3.088540 0.287060 0.961837
H -1.192911 -2.083304 -0.071555
H -0.348959 -2.528277 1.175066
H -1.404908 -0.277575 -1.583324
H 2.983377 -1.199507 1.483540
H -0.836872 1.190866 -1.555856
H 2.190400 -0.467601 2.605766
H 2.580161 1.981417 -0.034272
H 1.165232 2.337797 -0.614945
H 1.783446 -2.156469 -1.531151
H 2.422793 -0.825938 -1.998843
H -0.298033 1.186871 2.202228
H -2.164676 0.563406 1.230650
H -1.001754 3.648936 -0.493712
H -0.691186 2.293646 0.309569
H -3.307376 -1.989179 -1.281842
H -3.003412 -0.898262 -0.157556
H -3.667037 0.368429 1.726999

V(OH)2+(H2O)3

E = -1324.890223
O -0.464250 -0.976378 1.508120
V 0.000295 -0.084821 0.000062
O 0.465044 -0.976741 -1.507825
O 2.123476 0.046307 0.227293
O -2.123330 0.044667 -0.227558
O -0.001350 1.985726 -0.000336
H 0.115364 -1.445383 2.121995
H 2.504271 -0.479899 -0.496204
H -2.637395 -0.141649 -1.025275
H 2.637760 -0.139535 1.024994

H -2.503450 -0.482036 0.495919
H 0.783727 2.549618 0.044773
H -0.115676 -1.446215 -2.120325
H -0.788103 2.547333 -0.044866

V(OH)2+(H2O)4

E = -1401.335139
O -0.973003 1.688607 -0.956177
V -0.396430 -0.008321 0.072834
O -2.320236 -0.814358 -0.476690
O -1.055985 -0.297619 1.735083
O 1.308399 1.118893 0.539564
O 3.221138 -0.423155 -0.156337
O 0.657698 -1.278697 -0.733665
H -0.422785 2.482924 -1.011828
H -1.828211 1.859813 -1.374087
H 2.169574 0.645089 0.285076
H -2.735808 -1.088414 0.358207
H 1.438575 1.509315 1.413459
H -2.538135 -1.478333 -1.144624
H -0.571461 -0.214640 2.566909
H 2.606972 -1.050057 -0.583879
H 3.985052 -0.306389 -0.734267
H 0.310023 -2.117301 -1.064360

V(OH)2+(H2O)5

E = -1477.780428
O 0.967674 -1.165082 -0.883872
V -0.103815 0.392636 -0.093421
O -1.705584 -0.352487 -1.234156
O 0.010645 2.071235 -0.780532
O -1.068471 0.108729 1.445496
O 3.473801 -1.196322 0.148441
O -3.308752 -1.166170 0.589890
O 1.684321 0.968857 0.947200
H 1.896344 -1.381297 -0.638870
H 0.582489 -1.851789 -1.443898
H -2.480733 -0.669129 -0.665748
H -0.680657 2.523361 -1.281031
H -2.058984 0.097797 -2.010859
H 1.864400 1.893528 0.714993
H -2.751785 -0.721681 1.262074
H -0.687756 0.363906 2.296898
H -4.232811 -0.989446 0.802941
H 4.254767 -1.065848 -0.408819
H 3.742744 -1.845622 0.814561
H 2.510659 0.465504 0.846702

V(OH)2+(H2O)6

E = -1554.223167
O -0.345855 -1.474210 1.788127
V -0.234808 -0.531387 0.231892
O 1.182345 0.898790 0.010036
O 1.274484 -1.992828 -0.221504
O -1.284087 -1.032859 -1.201464
O -3.580522 0.345488 -0.872484
O -1.628835 0.986773 0.672218
O 3.567826 -0.382946 -0.718329
O 1.081283 3.538915 0.109218
H -1.059375 -1.391684 2.433508
H 2.194616 -1.712621 -0.380562
H -2.970266 -0.290772 -1.304966
H 1.272999 -2.605929 0.530539
H -1.022716 -1.808531 -1.715676
H 2.096480 0.675489 -0.253742
H 1.078363 1.885331 0.071997
H 4.349208 -0.366994 -0.147716
H 3.912439 -0.335073 -1.621443
H -2.470689 0.901946 0.120077
H 0.559777 4.087221 -0.490515
H 1.269411 4.085188 0.882772
H -1.893145 1.176038 1.580748
H -4.049620 0.825310 -1.565076

V(OH)2+(H2O)7

E = -1630.664045
 O -1.225273 0.975283 -0.900255
 V 0.060203 -0.523540 0.034835
 O 1.106791 1.297659 0.589000
 O -1.058840 -1.793767 -0.743177
 O 1.366893 -1.424403 1.021463
 O -1.332348 -0.310794 1.649250
 O 1.397585 -0.622841 -1.631715
 O 3.422314 -0.103020 0.062076
 O -3.320647 -0.673481 -0.115521
 O -0.450790 3.567762 -0.023327
 H -1.183004 1.912805 -0.636166
 H -2.158189 0.685085 -0.852621
 H 0.825307 2.211575 0.410449
 H 2.077732 1.219954 0.524519
 H -2.729130 -1.364940 -0.507762
 H 1.170222 -2.029026 1.745729
 H 1.236564 -0.116521 -2.437433
 H 2.322381 -0.454312 -1.337020
 H -1.213004 -0.767820 2.490618
 H -2.244044 -0.497193 1.323578
 H 2.949871 -0.775282 0.614589
 H -0.273443 4.263461 -0.671353
 H -4.238168 -0.947820 -0.227696
 H 4.371908 -0.227919 0.174045
 H -0.850895 4.019872 0.732493
 H -0.694239 -2.389678 -1.409522

HV(OH)₂+(H₂O)₇
 E = -1631.199186

O 0.954862 -1.954109 -0.206498
 V -0.402085 -0.712964 -0.310457
 O 0.746216 0.708702 -1.454033
 O -1.777665 -1.533112 0.351691
 O 0.624454 0.335294 1.239091
 O -1.687040 1.030869 -0.453504
 O -4.197553 -0.043661 0.254985
 O 2.957369 -1.023280 1.244393
 O -0.022040 3.034309 0.703992
 O 3.282343 0.833160 -0.753121
 H 2.368177 -1.650594 0.754372
 H 0.940274 -2.675198 -0.849402
 H 1.512582 -0.001309 1.498236
 H -4.827120 -0.215015 -0.459169
 H 0.629332 1.310383 1.226675
 H -4.737205 0.084741 1.046998
 H -2.613762 0.935706 -0.166372
 H -1.325269 1.872871 -0.121104
 H -2.713846 -1.258719 0.386339
 H 0.611945 0.600755 -2.403470
 H 1.733191 0.719065 -1.285099
 H -0.236615 3.710441 1.361047
 H 0.546320 3.474024 0.056337
 H 3.453603 -1.523910 1.902856
 H 4.065893 0.911727 -1.309682
 H 3.475475 0.157265 -0.070785
 H -0.682597 -1.159429 -1.843222

IR frequencies (in cm^{-1} , without shift) and intensities (KM/mole) for optimized structures

IIIa

29.2116 6.63
100.4123 27.9613
115.6578 9.0529
127.5987 0.7713
154.9182 101.0679
256.4148 0.8872
294.7278 69.7465
298.7716 0.0317
321.5702 23.7717
327.5694 157.8457
378.3872 83.5792
383.6366 135.821
471.6229 1.6006
497.5826 6.6675
500.6928 60.2387
1620.7903 158.5086
1626.4813 84.0752
1629.1639 117.9509
3742.5625 40.9156
3747.7323 61.9026
3769.9117 57.4104
3831.2512 138.508
3836.5109 177.7459
3871.9189 166.1723

IVa

44.4627 18.2648
48.6768 109.8995
61.1796 10.3131
72.0393 0.0327
94.0252 2.1339
120.9735 2.0443
135.6046 22.9128
152.6394 147.0518
171.3094 0.9112
217.0438 156.071
261.265 0.0692
268.7703 1.4151
285.5793 3.6592
320.4889 131.5965
331.2421 15.814
337.8662 37.1394
365.5608 172.8243
434.9625 0.0166
449.9725 0.0048
475.7373 0.0061
484.9311 48.9199
1615.4008 220.4813
1616.6203 45.151
1621.2947 131.8713
1625.0472 97.8528
3741.77 12.7396
3743.3627 12.5991
3757.5923 9.5001
3783.3327 52.3216
3835.5795 71.8137
3837.8748 136.7695
3852.0875 151.3951
3879.8655 134.8443

iIVa

87.097 0.1598
108.3064 3.2887
137.1009 6.1011
144.2954 7.0902
160.8182 18.435
213.4439 12.3564

244.3739 19.1611
320.9888 0.403
350.9581 146.9492
353.1423 30.2364
376.2187 9.6924
378.3559 82.8932
416.4697 203.2819
435.3377 163.6432
476.8875 120.2836
519.3671 100.4495
553.8967 149.985
566.3846 58.2565
579.2894 23.1244
634.4703 60.9039
691.6552 109.8973
760.1307 172.994
1620.7659 141.3335
1622.5389 11.6725
1625.1262 177.8241
1769.6226 181.9254
3716.7458 91.6611
3744.1504 95.8676
3749.2419 119.1102
3805.3278 104.0659
3817.4222 166.3532
3834.5071 161.8393
3843.816 193.5232

Va

32.9237 28.2167
45.2402 3.882
78.2181 0.3473
81.1911 0.2342
81.5809 16.3737
95.7964 2.1454
135.1324 4.2821
144.2206 32.1887
145.5624 2.7033
204.8959 1.5774
209.7341 34.4339
217.3749 20.4595
233.4548 314.7104
257.262 101.6293
276.8767 0.1047
288.3653 5.5347
290.1779 1.5139
316.8508 25.6155
355.3681 43.6392
355.6662 11.0391
433.0625 110.9896
441.8084 0.0736
444.1005 2.2618
556.8325 115.6597
616.7921 98.3348
619.7621 30.9262
672.1362 90.2829
1606.5089 92.2991
1609.8244 91.1149
1610.97 210.1004
1617.4893 101.7377
1655.6766 4.2414
3610.4294 71.5625
3641.4229 804.7842
3737.7826 3.5817
3738.21 5.2395
3764.5485 15.5152
3833.9546 1.2542
3835.4902 213.4392

3854.5208 196.3706
 3856.2098 92.0926
 3857.4376 124.9999

Vb

21.6662 0.28
 35.8649 11.4231
 45.3816 14.8264
 60.5851 3.5889
 81.8556 2.2224
 87.0322 6.3781
 103.5745 3.3766
 129.0041 83.894
 135.1881 25.9489
 144.4401 43.0649
 144.7843 108.0253
 208.0118 35.1177
 220.7977 18.2062
 273.3446 50.0383
 279.3072 51.9767
 291.6335 54.6325
 296.9954 26.7893
 318.4296 200.9197
 333.0714 65.4282
 351.226 71.4166
 354.389 127.8514
 375.6288 13.8073
 459.213 8.3538
 480.7629 1.9727
 499.4348 37.1697
 570.3715 23.977
 841.763 90.6142
 1612.2047 137.4586
 1621.5211 162.4664
 1623.2223 55.974
 1623.9774 31.9953
 1644.5413 98.5472
 3382.6882 1115.2107
 3735.1923 7.2919
 3749.6183 15.7497
 3755.5025 19.9802
 3792.6414 34.8981
 3818.5699 74.0355
 3831.2887 114.3775
 3844.5228 115.6927
 3850.3409 111.0474
 3894.9577 117.3446

Vc

18.7748 2.7385
 32.7532 4.7276
 44.8587 1.5019
 51.2566 1.911
 66.096 2.1835
 94.4042 4.3704
 102.5563 12.1973
 123.9884 52.6301
 130.4916 17.9298
 138.5002 40.8467
 145.0484 123.8932
 204.7683 212.4798
 231.0696 28.5659
 245.0419 27.9977
 271.0396 2.814
 297.8225 4.8116
 308.3309 11.3953
 322.6747 103.8551
 337.2626 86.2302
 363.6326 153.7401
 387.0562 62.5897
 438.5907 16.7959
 468.3519 1.2188
 618.8253 7.3703
 630.1283 29.8597
 823.0012 68.6093

884.4896 84.0305
 1616.2812 107.2775
 1618.5624 175.2674
 1619.1637 63.3799
 1642.3329 48.0606
 1649.868 25.2816
 3287.0869 1347.831
 3389.5181 1352.4732
 3745.9884 31.5181
 3790.452 35.4664
 3791.5513 39.53
 3813.9911 95.8137
 3828.7162 88.8254
 3838.8498 126.7149
 3892.501 118.2542
 3894.6214 127.3752

iVa

38.3333 1.2881
 49.7487 1.2891
 92.7497 5.4058
 113.4515 4.5279
 128.9751 5.3963
 142.5947 5.8748
 152.0293 5.3223
 170.4208 16.244
 185.6586 179.5454
 212.7936 4.8591
 247.442 94.7223
 268.1313 38.607
 316.1228 0.1836
 346.876 7.6371
 373.8642 17.1035
 396.473 66.08
 413.8249 258.2565
 432.0766 151.7773
 459.8412 76.3812
 473.6199 100.1538
 516.4997 113.415
 564.9828 93.5939
 581.3717 4.5567
 637.8671 32.0216
 691.3742 112.6218
 711.2859 69.7966
 752.199 174.9349
 961.4099 99.9182
 1614.1757 123.608
 1618.5005 21.0648
 1618.9856 168.1235
 1649.1354 40.0594
 1755.0419 207.6862
 3111.8835 1957.4626
 3717.6891 78.1272
 3748.2457 78.7949
 3786.3997 49.4949
 3815.3307 95.0964
 3817.1684 127.4316
 3829.0125 152.1785
 3840.2396 153.3302
 3887.2559 144.1114

iVb

43.9311 8.8577
 81.7001 0.3322
 113.8155 1.0327
 118.811 12.0222
 144.0091 3.9438
 152.3304 1.6531
 201.3793 59.1476
 222.1512 9.6143
 258.7883 82.7451
 310.9854 50.6202
 322.1758 109.8984
 325.8906 71.8592
 354.504 8.2128

375.0091 36.9845
 392.8141 20.9835
 403.0573 228.92
 411.0561 68.8154
 428.8181 77.0437
 454.1063 126.2364
 504.2976 11.9609
 530.2392 126.142
 546.6208 87.8144
 565.128 58.746
 630.0512 111.5075
 699.0425 90.3273
 719.7776 220.1977
 752.6026 64.3111
 1022.6555 111.0151
 1585.8614 92.6458
 1613.604 109.786
 1617.4368 132.6125
 1658.0016 59.4785
 1766.3108 179.3265
 2946.0426 1414.5904
 3667.9815 201.0837
 3748.6372 94.0194
 3751.8851 113.206
 3804.7599 91.7641
 3810.6042 128.9756
 3841.8322 151.1002
 3851.424 185.8704
 3862.3842 188.4397

iVc

45.1119 7.4196
 46.9501 7.5401
 92.569 53.0734
 106.2222 9.4026
 140.1239 2.2818
 155.346 11.0546
 171.1927 15.4665
 197.0965 28.3468
 223.1678 95.1071
 254.7795 20.4217
 284.6533 26.2249
 298.5148 93.7013
 319.2189 89.7448
 331.517 242.2255
 347.2029 46.1416
 368.9169 15.5501
 382.8287 27.5099
 411.9729 297.0964
 437.2261 6.8173
 484.2434 98.9121
 505.5352 78.8891
 534.5301 114.2556
 565.2844 31.6343
 605.5337 28.0313
 688.6908 195.2855
 697.1692 139.0004
 722.7203 47.0219
 1004.2316 115.8521
 1577.0744 97.9214
 1607.8119 127.716
 1616.2718 119.2332
 1646.3262 74.3919
 1755.4375 177.8988
 2975.3818 1393.527
 3701.3635 121.3952
 3756.0221 94.394
 3762.716 107.1008
 3797.2766 123.8363
 3817.4332 141.4961
 3852.3884 157.4435
 3862.7875 170.4785
 3869.1162 192.7617

VIa

23.7803 1.6819
 36.2283 1.1314
 55.668 11.6028
 69.3366 0.2602
 79.1236 0.1406
 91.5242 0.005
 93.9687 3.042
 98.0657 11.1213
 108.1642 32.7231
 127.3656 120.0966
 143.522 59.7691
 153.6604 45.9929
 174.8071 1.847
 205.7425 64.2545
 207.0362 122.7595
 229.215 108.8974
 232.3448 234.6862
 278.8178 1.4162
 288.6414 6.706
 293.8644 30.7402
 303.0003 31.6125
 307.1226 9.8339
 358.7482 43.5765
 363.0474 8.6022
 392.314 17.9595
 427.723 3.6858
 436.0404 3.3797
 436.1651 0.4862
 591.8377 77.9827
 656.329 125.0418
 660.9725 10.2611
 777.273 78.1911
 903.2662 94.7481
 1603.1706 81.1385
 1607.5357 202.0287
 1610.3229 91.0929
 1621.8556 94.1909
 1628.3804 36.7709
 1670.642 13.1255
 3398.8988 1582.1759
 3482.6994 144.116
 3547.5435 760.9129
 3735.71 8.2755
 3736.0779 1.411
 3794.4284 32.1325
 3833.2941 0.0287
 3834.1171 63.9927
 3834.7469 223.415
 3855.1043 171.7601
 3856.0068 61.8886
 3896.8222 119.2295

VIb

11.8195 0.2839
 30.1653 6.9128
 39.6496 7.8205
 67.5391 5.5572
 77.1071 7.8788
 83.9911 1.6781
 93.118 2.2503
 115.0158 12.9161
 126.9412 12.5495
 131.955 8.1634
 146.6623 3.137
 159.8675 56.2277
 209.7195 23.8758
 210.901 48.0604
 217.424 18.9233
 226.8052 87.942
 246.6378 63.0881
 264.4743 199.6587
 277.9527 6.6119
 280.3146 5.3879
 301.6642 106.5802
 311.3797 4.8498

335.3601 76.034
 350.1947 14.5621
 376.1232 49.0046
 426.1438 116.0321
 445.6556 4.3922
 537.0726 78.7887
 592.1063 136.9569
 601.4648 14.6198
 626.4354 41.8101
 680.1253 64.2015
 739.8513 71.6463
 1602.6884 141.2648
 1605.7475 81.459
 1615.8261 125.8831
 1622.8813 98.8092
 1651.0203 10.9336
 1653.2152 61.2325
 3421.9971 897.4996
 3619.3969 69.5829
 3647.2058 681.2575
 3725.6285 10.3824
 3765.1274 12.2985
 3785.7309 23.1531
 3818.9413 68.2359
 3824.1495 105.7356
 3846.3932 146.3859
 3851.8945 131.7843
 3859.2292 117.9671
 3886.9523 107.1743

iVIa

32.1944 6.8225
 55.2065 1.5771
 93.495 0.4553
 93.9865 0.3114
 130.5842 2.5289
 138.6049 2.778
 155.7363 1.0915
 165.9196 1.3104
 218.2973 77.2433
 240.0969 19.1781
 254.2858 34.8168
 278.2301 56.9201
 298.0415 23.3485
 314.2148 74.2958
 328.76 84.8735
 336.7782 19.8731
 363.1573 64.1237
 394.8108 41.0072
 403.5772 23.4222
 421.4414 41.4927
 446.5793 210.5184
 467.4763 104.3309
 483.5944 69.0686
 522.9733 17.4871
 553.4829 111.2266
 588.3446 96.0895
 596.7959 45.6064
 663.6662 175.153
 695.0132 80.3332
 717.0352 78.4774
 736.0111 166.985
 779.5661 113.6259
 794.9983 192.4302
 1021.3076 106.3065
 1592.6977 89.4297
 1599.672 110.7595
 1622.8289 112.6956
 1655.0699 29.2853
 1664.4369 51.3179
 1757.8149 202.9634
 2972.8025 1335.4955
 3450.0437 734.9057
 3606.6225 370.8213
 3639.4705 482.1564

3756.3026 36.0231
 3794.6512 88.0034
 3817.2339 120.3338
 3819.2987 232.7647
 3825.0487 142.8995
 3845.2693 146.7256
 3860.2157 163.4348

VIIIa

9.4753 2.3495
 27.1885 2.721
 27.8463 0.0411
 36.0862 0.2255
 43.617 4.5563
 72.2596 0.1306
 76.0583 3.1388
 81.1432 0.6452
 88.6541 2.7146
 93.7257 0.9765
 94.4083 4.6185
 122.0332 145.7625
 129.6427 65.8024
 137.4448 63.1863
 145.0539 208.3711
 157.8576 0.1281
 173.9422 0.2146
 187.5461 23.0832
 202.3764 61.6703
 231.9433 0.1193
 253.4314 5.4893
 280.5952 96.0711
 286.0396 9.2735
 286.1451 0.5452
 289.0041 39.8236
 300.5241 7.2092
 303.1256 219.4155
 304.9151 8.7834
 332.1645 11.8087
 355.2419 58.8026
 355.5837 4.2002
 369.4585 4.3237
 402.5385 103.9606
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3835.214 91.9667
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3897.9432 125.3426

VIIIb

13.7134 2.9293
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iVIIIa

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iVIIIb

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iVIIIc

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IXa

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IXb

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IXd

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iIXa

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iIXc

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